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Examination in Statistical Image Analysis, August 20, 2015

Course code Chalmers: TMS016, Gothenburg University: Statistisk Bildbehandling, MSA300

Written examination August 20, 2015, 8.30–12.30.

Literature and notes may be brought for this written examination. Neither pocket calculators nor computers are allowed at this examination. In the written examination there are two pages and two problems. You are supposed to answer both problems, and in the judgement they have the same weight. Answers may be given in English or Swedish.

Problem 1.

Figure 1 shows part of an image of a spruce tree forest photographed from an airplane about 560 m above the forest. For each tree the tree top is seen more or less clearly. One is interested in finding the positions in a horizontal plane of the tree tops. (We disregard here the vertical position of the tree tops).

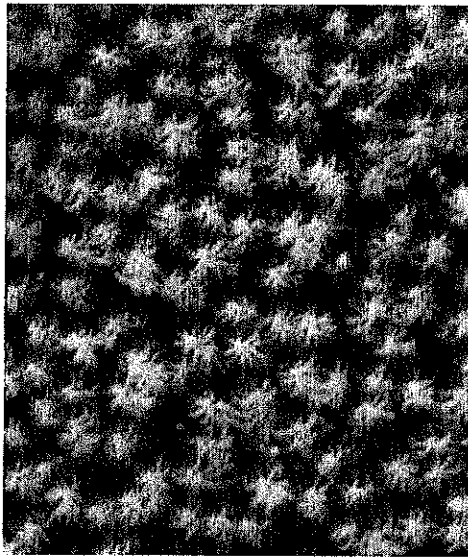


Figure 1: Part of a forest of spruce trees photographed from above.

- a) Describe a method based on image smoothing for finding the tree top positions. To start with, disregard possible edge effects, that is problems associated with smoothing near the edges of the image.
- b) Suppose now that you have found the tree top positions. Describe how you can test if the estimated tree top positions form a Poisson process with constant intensity. Looking at the image, do you expect that a Poisson process gives a good description of the data?
- c) Discuss now how you may improve the smoothing discussed above in a) by taking care of edge effects in some way.

Problem 2.

Suppose now that in addition to the data in Figure 1 you have the true planar positions of the tree tops measured from the ground. One is interested in evaluating the method described above to estimate the tree top positions from images obtained from an airplane.

a) Suppose first that you for each estimated tree top can associate which true tree top it corresponds to. How can you then characterize the estimation method, for instance in terms of a distribution for the measurement error? Give suitable formulas.

b) Suppose now that you have the point process of estimated tree positions and the point process of true tree positions but you do not know which true tree top that corresponds to a given estimated tree position. Discuss how you can then characterize the accuracy of the method of estimating tree top positions from airplane images. If you wish you may start by assuming that there are equally many points in the two sets of estimated and true tree positions. Then you can proceed to the case that the two numbers may differ.