

Q1.

a.p1, p2 (writes 0), q1, q2, p2 (writes 2), p1 (exits).

b.q1, q2, p1 produces no output, and both halt.

c.The value 2 can appear only once, because the value of n can only increase. So if p2: write(n)

is executed with n = 2, the subsequent execution of p1: while n < 2 prevents another execution

of p2.

d.q1 followed by (p1, p2)\* but fairness says q2 has to run sometime, so then p1 exits. So 1 can appear a finite number of times.

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Question 2.

(a) See textbook, p. 152.

(b) Three, one for each condition variable, and one for monitor entry.

(c) Like (a), but remove condition variables. Guard entry `put` by `when buffer not full` and entry `get` by `when buffer not empty`.

The bodies of the entries need no `if` or `signal`.

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Question 3.

(Part a)

The table is:

	State=(p <sub>i</sub> , q <sub>i</sub> , S)	next state if p moves	next state if q moves
1.	(p <sub>2</sub> , q <sub>2</sub> , Z)	(p <sub>3</sub> , q <sub>2</sub> , P)	(p <sub>2</sub> , q <sub>3</sub> , Q)
2.	(p <sub>2</sub> , q <sub>3</sub> , Q)	(p <sub>3</sub> , q <sub>3</sub> , QP)	(p <sub>2</sub> , q <sub>5</sub> , Q)
3.	(p <sub>2</sub> , q <sub>5</sub> , Q)	(p <sub>3</sub> , q <sub>5</sub> , QP)	(p <sub>2</sub> , q <sub>2</sub> , Z)
4.	(p <sub>3</sub> , q <sub>2</sub> , P)	(p <sub>5</sub> , q <sub>2</sub> , P)	(p <sub>3</sub> , q <sub>3</sub> , PQ)
5.	(p <sub>3</sub> , q <sub>3</sub> , PQ)	(p <sub>5</sub> , q <sub>3</sub> , PQ)	no move
6.	(p <sub>3</sub> , q <sub>3</sub> , QP)	no move	(p <sub>3</sub> , q <sub>5</sub> , QP)

- 7. (p3, q5, QP)                    no move                    (p3, q2, P)
- 8. (p5, q2, P)                    (p2, q2, Z)                    (p5, q3, PQ)
- 9. (p5, q3, PQ)                    (p2, q3, Q)                    no move

(Part b) There is no state with (p5, q5, S)

(Part c) Every state has at least one move.

(Part d).

Prove that every p2-state leads to a p5-state.

By definition, 8 and 9 are in M.

5 has to lead to 9. So  $M = \{5, 8, 9\}$

4 leads to 8 or 5. So  $M = \{4, 5, 8, 9\}$

6 and 7 have to lead to 4. So  $M = \{4, 5, 6, 7, 8, 9\}$

1-2-3 can loop by doing only q moves. By fairness, one of them must do a p step at some point,

leading to 4, 6, or 7.

So  $M = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$ .

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Question 4.

Let  $M_p = p4 \wedge (S=P \vee S=PQ)$ .

4a. Show that  $M_p$  is invariant.

If  $\neg p4$ ,  $M_p$  holds.

Can p arrive at p4 when the consequent is false?

p4 can only happen if p does p3.

Then the await ensures  $(S = P \vee S = PQ)$ .

Suppose p is at p4, the consequent is true, and then q spoils it.

But only q2 and q5 assign to S.

$(S = P \vee S = PQ)$  followed by q2 yields  $S=PQ$ .

$(S = P \vee S = PQ)$  followed by q5 also yields  $S=P \vee S=PQ$ .

So  $\square M_p$

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4b. Show mutex,

$M_q = q_4 - (S=Q \vee S=QP)$ .

$p_4 \ \& \ q_4$  - false (no agreement on S).

So no such state exists.

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4c. Show that there cannot be deadlock.

Suppose  $[(p_3 \ \& \ q_3)]$ . Then both awaits wait. So  $S=Z$ .

But after  $p_2$  or  $q_2$  (one of them must be the last thing before  $p_3 \ \& \ q_3$ ),

S cannot remain Z, and neither produces Z.

So S is P or QP or Q or PQ.

So  $[(p_3 \ \& \ q_3)]$  is impossible.

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Question 5. The thing to realise is that W carries a charge of +2, G carries a charge of +1, and B a charge of -1. Then val is the excess charge.

There is a conservation of charge, because the values w, b, g change only in lines 15 and 20. Line 15 follows removal of W and B and posting of G, so it reflects the

charge correctly. Line 20 follows removal of G and B.

The computation continues until only the excess charge remains, all balancing charges having been removed. That is what lines 33 and 34 do.

a.  $MaxW=MaxB=3$  means  $val = 2*3 - 3 = 3$ . So the only possibilities are  $w=1, g=1$  or  $g=3$ .

Remove (W), Remove(B), Post(G) thrice, i.e.,  $W+B - G, W+B - G, W+B-G$  gives the latter.

Any process could do this, because the W has to be removed first, and the B cannot be stolen by someone without a B.

Do Remove(W), Remove(B), Post(G), Remove(W), Remove(B), Post(G). Interpolate Remove(G), Remove(B) sequences. This gives  $w=1, g=1$ .

b. Val is invariant. See above.

c. Termination. See above.

d. Consider  $MaxW=MaxB=1$ . The only result should be  $W+B-G$ . But with two R  ms, we could have R1 taking W and R2 taking B, followed by both timing

out and replacing the W and B. Loop.

The whole question illustrates how to avoid deadlock/livelock in resource allocation by imposing an order on the resources. There is no need for synchronization between the Rs, so the Linda is almost irrelevant.

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Question 6.

a. Write I for Ints, E for End, and C(c) for Cell holding c. Show links with the name of the channel between daxes.

I â€“qinit- E

After 34,

I â€“qinit- C(34) â€“q- E

After 76

I â€“qinit- C(34) â€“qout- C(76) â€“q- E

After 23

I â€“qinit- C(23) â€“q- C(34) â€“qout- C(76) â€“q- E. We might want to use notation or colours to show whose local channel goes where.

The program as a whole does an insertion sort, printing out the sorted list as a 0 goes through the chain of processes.

b. CAP has no effect.

c. Add the line

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n == c- run Cell (c, qin, qout)
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as one of the branches of the if in Cell.

d.

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:: n==0 - printf("%d\n", c);  
    qout ! 0;  
    run Cell (c, qin, qout)
```

is the change to be made to the branch n==0.