

Lösningar elektronik aug 2016

1a Kondensatorer har även induktans och resistans.

1b filter: stabil kapacitans, små förluster

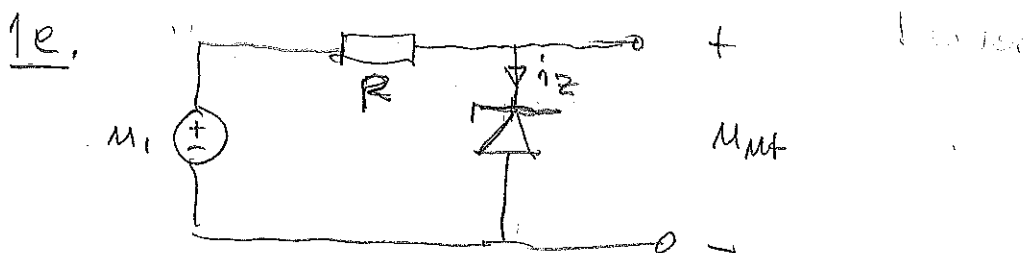
Koppling: Låg impedans över stort frekvensområde.

1c Diod: Likriktning

Z-diod: Spänningsstabilisering

1d. $T_j - T_a = P_f \cdot \Theta_{ja} \Rightarrow 150^\circ\text{C} - T_a = 1\text{W} \cdot 62,5^\circ\text{C/W} \Rightarrow$

$T_a = 87,5^\circ\text{C}$

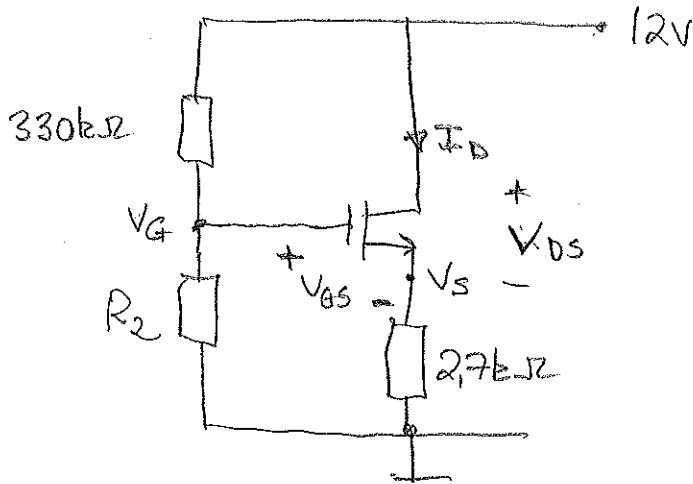


Stabil $U_M \Leftrightarrow i_Z \geq 0 \Rightarrow U_1 \geq E_Z = \underline{10\text{V}}$

$U_{1\text{max}}$ ges av $i_Z \leq \frac{P_Z}{E_Z} = \frac{0,5\text{W}}{10\text{V}} = 50\text{mA} \Rightarrow$

$U_{1\text{max}} = E_Z + R \cdot i_{Z\text{max}} = 10\text{V} + 100\Omega \cdot 50\text{mA} = \underline{15\text{V}}$

1F.



$$V_E = 2V$$

$$k = 4 \text{ mA/V}^2$$

$$g_m = 4 \text{ mA/V}$$

$$g_m = \sqrt{2kI_D} \Rightarrow I_D = \frac{g_m^2}{2k} = \frac{(4 \text{ mA/V})^2}{2 \cdot 4 \text{ mA/V}^2} = \underline{2 \text{ mA}}$$

$$\Rightarrow V_S = 2,7 \text{ k}\Omega \cdot 2 \text{ mA} = \underline{5,4 \text{ V}}$$

$$2 \text{ mA} = \frac{4 \text{ mA/V}^2}{2} (V_{GS} - 2 \text{ V})^2 \Rightarrow$$

$$V_{GS} = \pm 1 \text{ V} + 2 \text{ V} = \begin{cases} 1 \text{ V} & (\text{strykt; ty } V_{GS} < V_E \\ 3 \text{ V} \end{cases}$$

$$V_{DS} = 12 \text{ V} - V_S = 6,6 \text{ V} > V_{GS} - V_E = 1 \text{ V} \Rightarrow$$

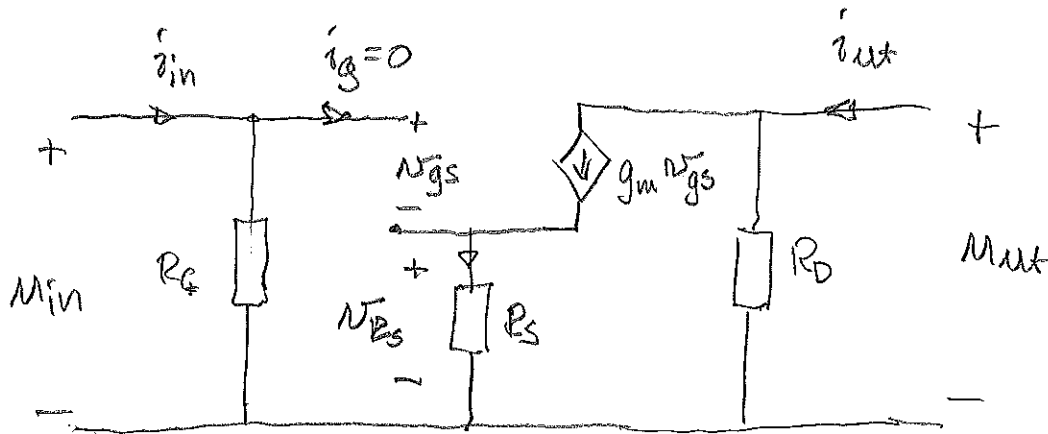
strömmättnad!

$$V_G = V_{GS} + V_S = 3 \text{ V} + 5,4 \text{ V} = 8,4 \text{ V}$$

$$V_G = \frac{R_2}{R_2 + 330 \text{ k}} \cdot 12 \text{ V} = 8,4 \text{ V} \Rightarrow$$

$$1 + \frac{330 \text{ k}}{R_2} = \frac{12 \text{ V}}{8,4 \text{ V}} \Rightarrow \underline{\underline{R_2 = 770 \text{ k}\Omega}}$$

2 (aug 2016) Swa signal schema



$$R_D = 1,2 \text{ k}\Omega \quad R_S = 200 \Omega \quad R_G = 560 \text{ k}\Omega \quad g_m = 7 \text{ mA/V}$$

$$\underline{R_{in}} = R_{iu} = \left. \frac{v_{in}}{i_{in}} \right|_{i_{out}=0} = \underline{\underline{R_G = 560 \text{ k}\Omega}}, \text{ ty } i_g = 0.$$

$$\left. \begin{array}{l} \frac{v_{out}}{v_{in}} \\ i_{out}=0 \end{array} \right\} \begin{array}{l} v_{in} = v_{gs} + R_S \cdot g_m v_{gs} = (1 + g_m R_S) \cdot v_{gs} \\ v_{out} = -g_m R_D v_{gs} \end{array} \Rightarrow$$

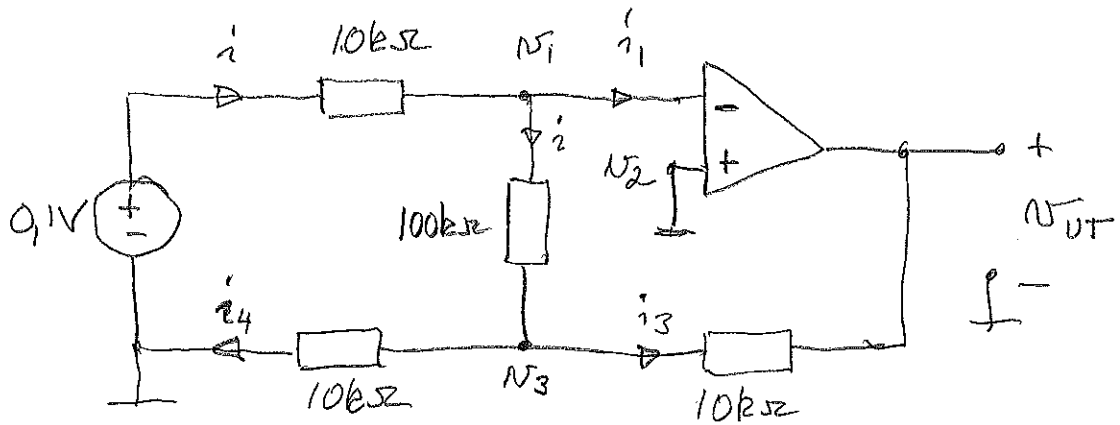
$$\frac{v_{out}}{v_{in}} = - \frac{g_m R_D}{1 + g_m R_S} = \underline{\underline{-3,599}}$$

$$R_{out} = \left. \frac{v_{out}}{i_{out}} \right|_{v_{in}=0} \quad v_{in} = 0 \Rightarrow v_{gs} = -v_{gs}$$

$$\text{Men } v_{R_S} = g_m R_S \cdot v_{gs}, \text{ sa } -v_{gs} = g_m R_S v_{gs} \Rightarrow$$

$$v_{gs} = 0 \Rightarrow i_{out} = \frac{v_{out}}{R_D} \Rightarrow \underline{\underline{R_{out} = R_D}}$$

3



Ideal motkopplad OP $\Rightarrow i_1 = 0, U_1 = U_2 = 0$

Rin

$$i_1 = \frac{0,1V - U_1}{10k} = \frac{0,1V - 0V}{10k} = 10\mu A$$

$$R_{in} = \frac{0,1V}{i_1} = \underline{\underline{10k\Omega}}$$

Uout : $U_{out} = U_3 - 10k\Omega \cdot i_3$

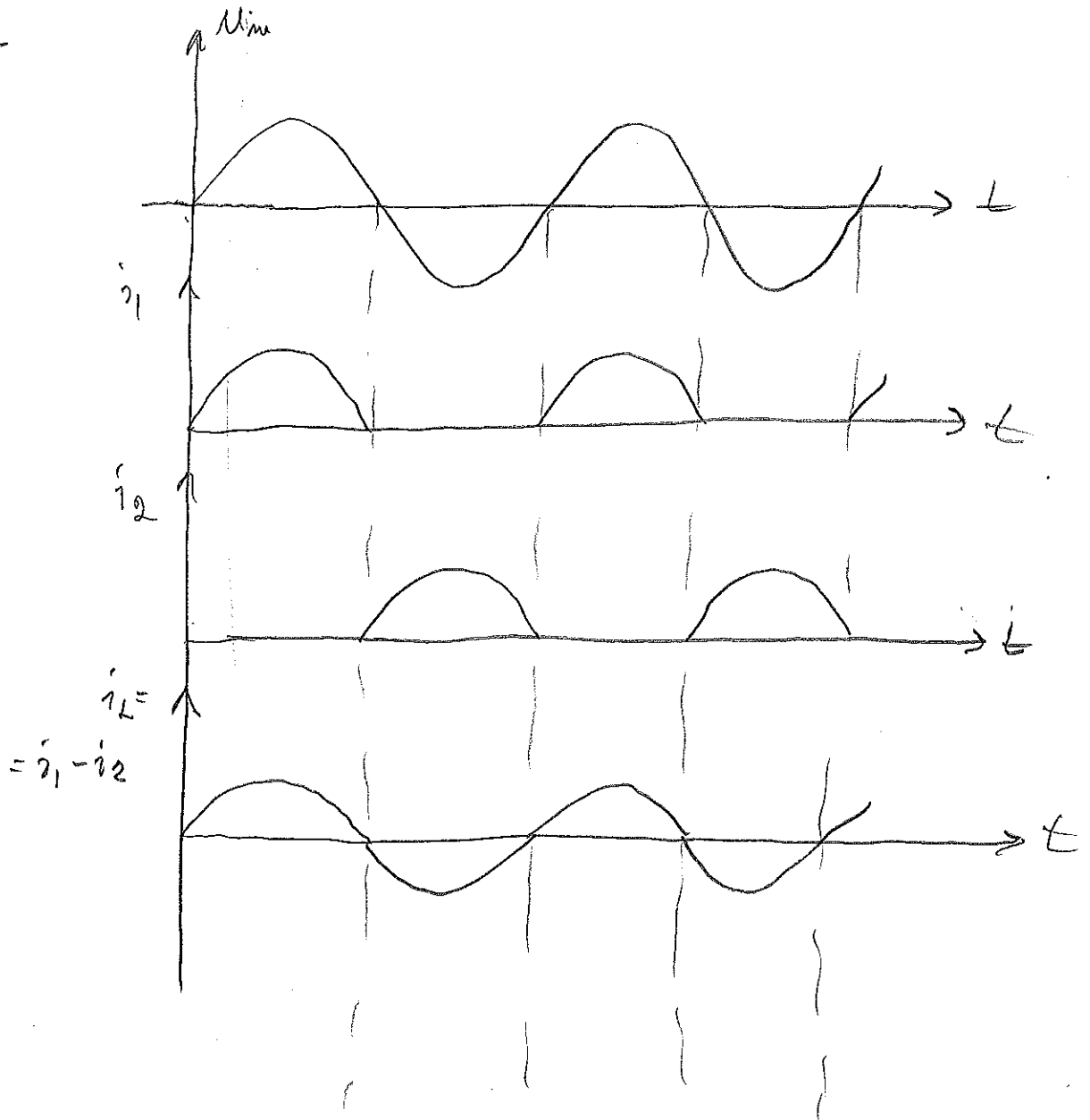
$$U_3 = U_1 - 100k\Omega \cdot i_1 = 0 - 100k\Omega \cdot 10\mu A = -1V$$

$$i_4 = \frac{U_3}{10k\Omega} = \frac{-1V}{10k\Omega} = -100\mu A$$

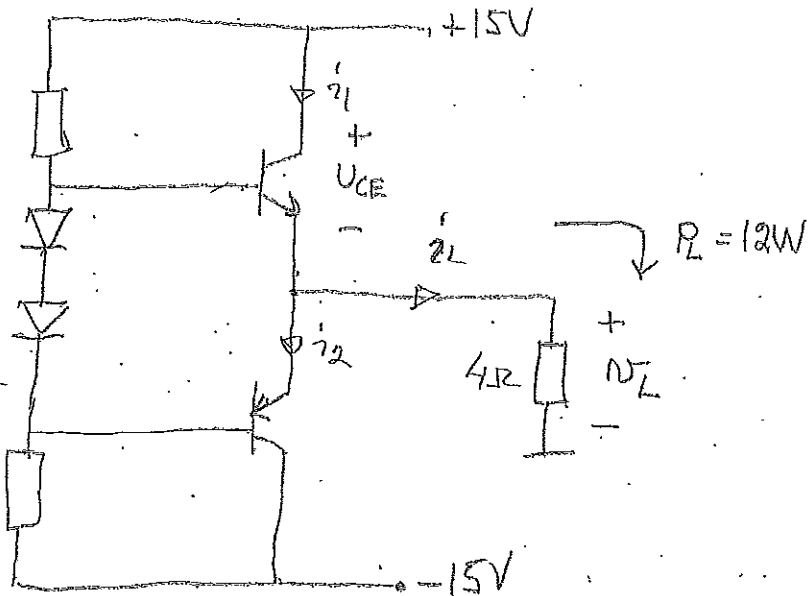
$$i_3 = i_1 - i_4 = 10\mu A - (-100\mu A) = 110\mu A$$

$$\Rightarrow U_{out} = -1V - 10k\Omega \cdot 110\mu A = \underline{\underline{-2,1V}}$$

4a



4b



$$P_L = 4\Omega \cdot \frac{i_L^2}{2} \Rightarrow \frac{i_L}{2} = \sqrt{\frac{2 \cdot 12W}{4\Omega}} = \underline{2,45A}$$

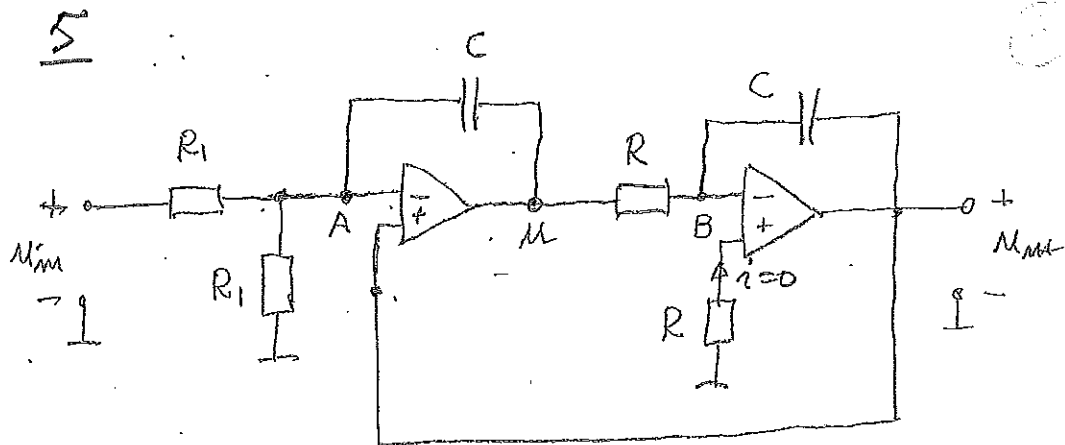
$$\Rightarrow i_1 = \underline{2,45A}$$

$$P_{im} = 2 \cdot 15V \cdot \frac{i_1}{\pi} = 30V \cdot \frac{2,45A}{\pi} = \underline{23,39W} \Rightarrow$$

$$\eta = \frac{P_L}{P_{im}} = \frac{12W}{23,39W} = \underline{51,3\%}$$

$$P_{T\text{-transistor}} = \frac{P_{im} - P_L}{2} = \underline{5,70W}$$

$$P_{L\text{max}} = \frac{(V_{L\text{max}})^2}{2 \cdot 4\Omega} = \frac{(15V)^2}{2 \cdot 4\Omega} = \underline{28,1W}$$



Ideala matkoppade OP \Rightarrow

- instömmar = 0
- lika potential på ingångarna.

$$\Rightarrow V_A = u_{out} \quad ; \quad V_B = 0$$

Nodanalys:

$$\underline{A} \quad \frac{V_A - u_{in}}{R_1} + \frac{V_A}{R_1} + \frac{V_A - M}{1/sC} = 0 \quad ; \quad V_A = u_{out} \Rightarrow$$

$$(2 + sRC) \cdot u_{out} = sR_1C \cdot M + u_{in} \quad (1)$$

$$\underline{B} \quad \frac{V_B - M}{R} + \frac{V_B - u_{out}}{1/sC} = 0 \quad ; \quad V_B = 0 \Rightarrow$$

$$M = -sRC \cdot u_{out} \quad (2) \quad ; \quad \text{sätt in i (1)}$$

$$(2 + sRC) \cdot u_{out} = -s^2 R R_1 C^2 + u_{in} \Rightarrow$$

$$\frac{u_{out}}{u_{in}} = \frac{1}{s^2 R R_1 C^2 + sRC + 2} = \frac{1}{R R_1 C^2} \cdot \frac{1}{s^2 + \frac{1}{RC} s + \frac{2}{R R_1 C^2}}$$

$$\text{Polar: } s^2 + \frac{1}{RC} s + \frac{2}{R R_1 C^2} = 0 \Rightarrow$$

$$s = -\frac{1}{2RC} \pm \sqrt{\frac{1}{4R^2C^2} - \frac{2}{R R_1 C^2}}$$

Maximalt snabbt utan översväng \Rightarrow

$$\frac{1}{4R^2C^2} = \frac{2}{R_1C^2} \Rightarrow R_1 = 8R = \underline{\underline{80k\Omega}}$$

Då gäller att

$$\frac{M_{\max}}{M_{\min}} = \frac{1}{R_1C^2} \cdot \frac{1}{\left(s + \frac{1}{8RC}\right)^2} = 56,6 \cdot 10^6 \cdot \frac{1}{(s + 10638)^2} =$$

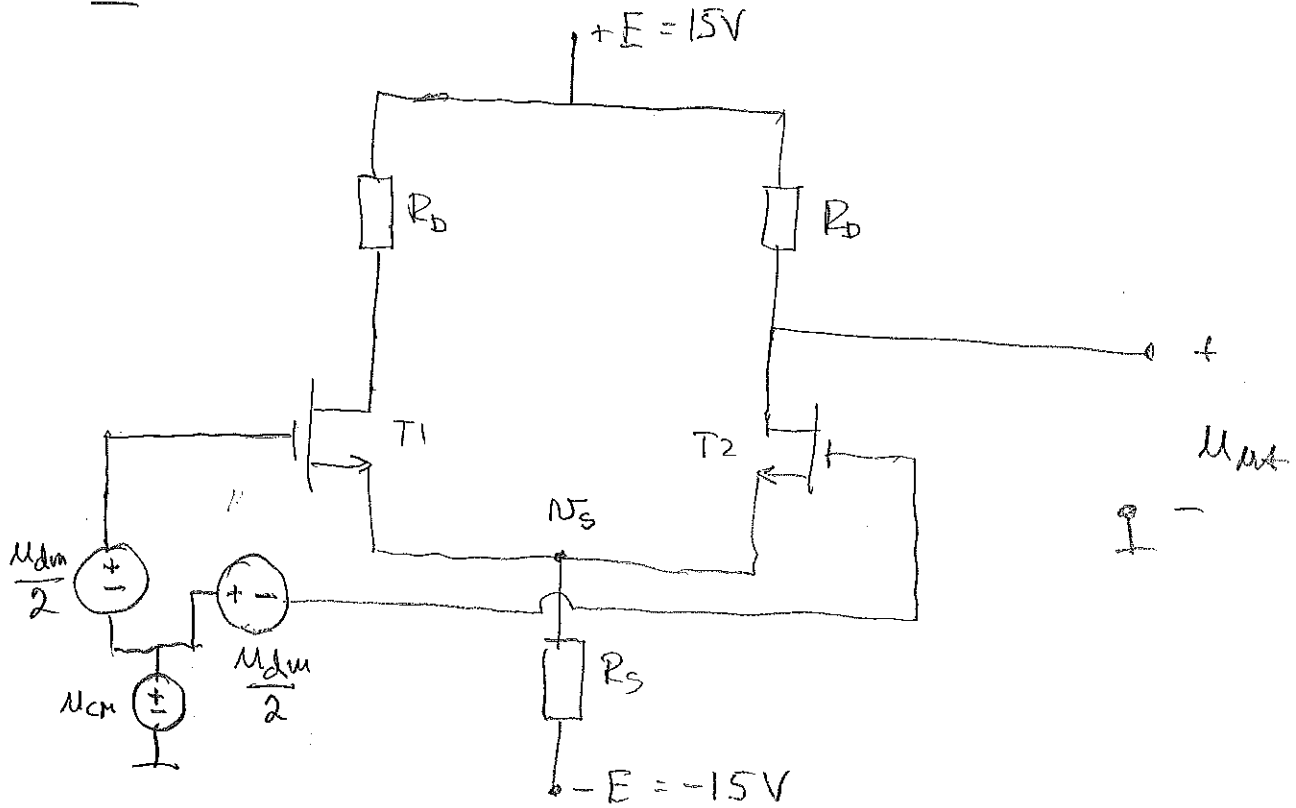
$$= \frac{0,5}{\left(1 + \frac{s}{10638}\right)^2} \cdot \text{Dubbelpol } s = -10638 \Rightarrow$$

$$\omega_{\text{TOT}} = 10638 \text{ rad/s} \cdot \sqrt{2^{1/2} - 1} = 6847 \text{ rad/s} \Rightarrow$$

$$\text{Övre gränshfrekvens } f_0 = \frac{6847}{2\pi} \text{ Hz} = 1089,7 \text{ Hz}$$

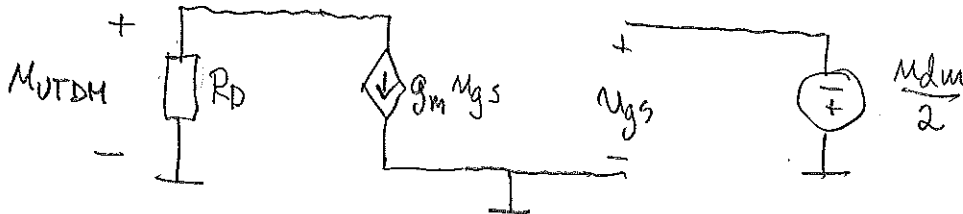
$$\Rightarrow \text{Stigtiden } t_r = \frac{0,35}{f_0} = \underline{\underline{0,32 \text{ ms}}}$$

6



$R_D = 10\text{k}\Omega$ $R_S = 3,3\text{k}\Omega$ $g_m = 10\text{mA/V}$

DH : $U_{cm} = 0$ $U_S = 0$ Betrachte T2

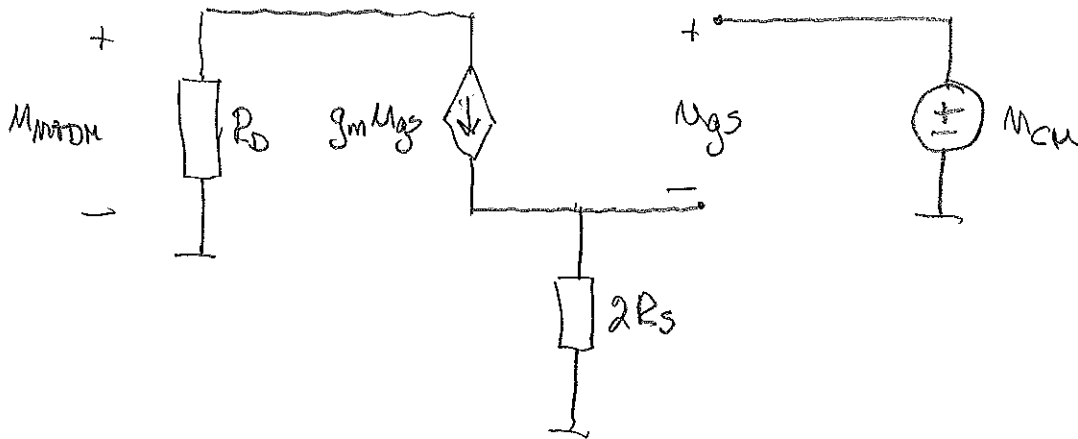


$U_{outDH} = -g_m R_D U_{gs}$; $U_{gs} = -\frac{U_{dm}}{2} \Rightarrow$

$U_{out} = g_m R_D \cdot \frac{U_{dm}}{2} \Rightarrow$

$A_{dm} = \frac{U_{outdm}}{U_{dm}} = \frac{g_m R_D}{2} = \underline{50g_m R}$

CM : $u_{dm} = 0$, Betrachte T2



$$u_{outCM} = -g_m R_D u_{gs}$$

$$u_{cm} = u_{gs} + 2g_m R_S \cdot u_{gs} = (1 + 2g_m R_S) \cdot u_{gs} \Rightarrow$$

$$A_{cm} = \frac{u_{outCM}}{u_{cm}} = -\frac{g_m R_D}{1 + 2g_m R_S} = -1,4999$$

$$CMRR = 20 \cdot \log \left| \frac{A_{dm}}{A_{cm}} \right| = 20 \cdot \log \frac{50}{1,49} = \underline{\underline{30,5 \text{ dB}}}$$
