

Svar Elektroteknik 3 juni 2016

1a.
$$P_{f_{max}} = \frac{150^\circ - 40^\circ}{2^\circ\text{C/W} + 20^\circ\text{C/W}} = \underline{\underline{5\text{W}}}$$

1b. Metallfilmatstånd har induktans
Kälmassamotstånd har brus

1c.
$$\omega_0 = (1 + \beta A) \cdot 25 \text{ rad/s} = \left(1 + \frac{1\text{k}}{1\text{k} + 99\text{k}} \cdot 10^5\right) \cdot 25 \text{ rad/s} \approx$$

$$\approx \underline{\underline{25,03 \text{ krad/s}}}$$

1d.
$$i_D = \frac{16\text{V} - 12\text{V}}{1\text{k}\Omega} = 4\text{mA} ; 4\text{mA} = \frac{4\text{mA/V}^2}{2} (V_{GS} - 3\text{V})^2 \Rightarrow$$

$$V_{GS} = 4,41\text{V} ; V_S = 10\text{V} - V_{GS} = 5,59\text{V} \Rightarrow$$

$$R_S = \frac{5,59\text{V}}{4\text{mA}} \approx \underline{\underline{1,40\text{k}\Omega}}$$

1e. primärbatterier är ej laddningsbara
Sekundärbatterier är laddningsbara

1f. Reella poler! $s^2 + 9bs + 5 = 0 \Rightarrow$

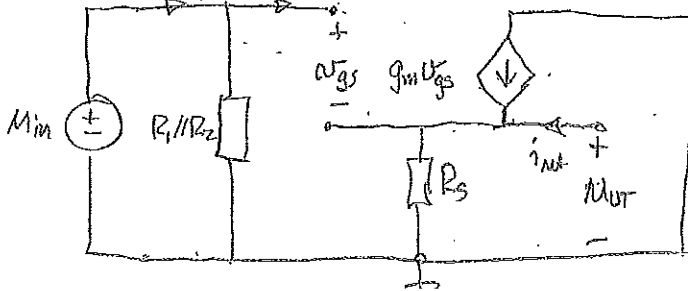
$$s = -4b \pm \sqrt{16b^2 - 5} \Rightarrow \underline{\underline{|b| > \frac{\sqrt{5}}{4} = 0,559}}$$

2. $U_+ = 187,2 \text{ mV}$.

$$\frac{U_- + 0,1 \text{ V}}{6,8 \text{ k}} + \frac{U_- - U_0}{100 \text{ k}} = 0 \quad U_- = U_+ = 187,2 \text{ mV} \Rightarrow$$

$$\underline{\underline{U_0 = 4,41 \text{ V}}}$$

3. i_{in} $i_g = 0$



$$U_{in} = U_{gs} + g_m U_{gs} R_s, \quad U_{out} = g_m U_{gs} R_s \Rightarrow$$

$$\frac{U_{out}}{U_{in}} = \frac{g_m R_s}{1 + g_m R_s}, \quad g_m = \sqrt{2k \cdot I_D} = 4 \text{ mA/V} \Rightarrow$$

$$\underline{\underline{\frac{U_{out}}{U_{in}} = \frac{8}{9} \approx 0,89}}$$

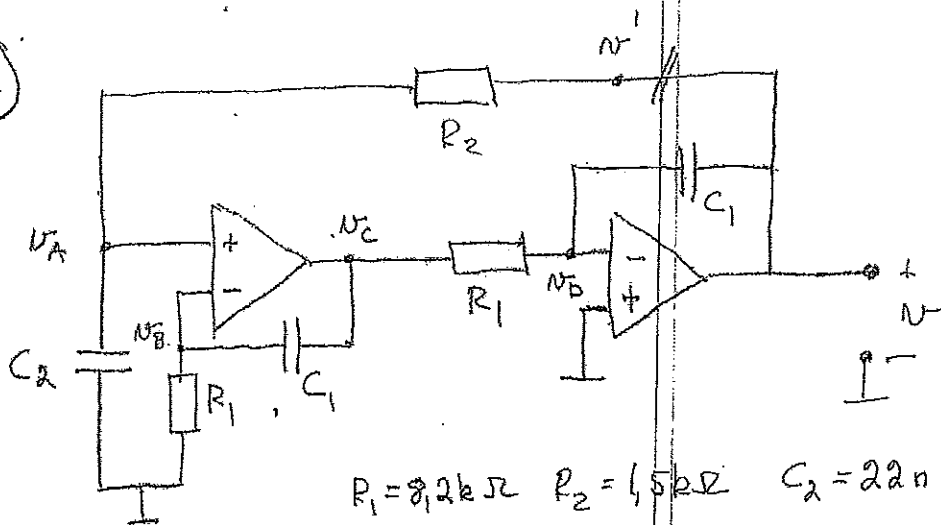
$$R_{in} = \frac{U_{in}}{i_{in}} = R_1 // R_2 = \underline{\underline{68,75 \text{ k}\Omega}}$$

$$R_{out} = \left. \frac{U_{out}}{i_{out}} \right|_{U_{in}=0}, \quad U_{in}=0 \Rightarrow U_{out} = -U_{gs}$$

$$U_{out} = R_s (i_{out} + g_m U_{gs}) = R_s (i_{out} - g_m U_{out}) \Rightarrow$$

$$R_{out} = \frac{R_s}{1 + g_m R_s} \approx \underline{\underline{222 \Omega}}$$

4.



$$R_1 = 8,2 \text{ k}\Omega \quad R_2 = 1,5 \text{ k}\Omega \quad C_2 = 22 \text{ nF}$$

Ideala motkopplade OP \Rightarrow • instömmar = 0

$$\bullet U_A = U_B; U_D = 0$$

Teckna $T(s) = \frac{U}{U_A}$ och lös

ekvationen. $T(j\omega) = 1$.

Nodanalys: $U_A - U' + \frac{U_A}{1/sC_2} = 0 \Rightarrow$

$$U_A = \frac{U'}{1 + sR_2C_2} \quad (1)$$

$$\frac{U_B}{R_1} + \frac{U_B - U_Z}{1/sC_1} = 0 \Rightarrow U_B = \frac{sR_1C_1}{1 + sR_1C_1} \cdot U_Z \quad (2)$$

$$(1) \text{ och } (2) \text{ ger } U' = \frac{sR_1C_1(1 + sR_2C_2)}{1 + sR_1C_1} \cdot U_Z \quad (3)$$

$$\frac{U_D - U_Z}{R_1} + \frac{U_D - U}{1/sC_1} = 0; U_D = 0 \Rightarrow$$

$$U_Z = -sR_1C_1 \cdot U \quad (4)$$

(3), (4) ger nu att

$$U^1 = -s^2 R_1^2 C_1^2 \cdot \frac{1+sR_2C_2}{1+sR_1C_1} U \Rightarrow$$

$$T(s) = \frac{U}{U^1} = - \frac{1}{s^2 R_1^2 C_1^2} \cdot \frac{1+sR_1C_1}{1+sR_2C_2} \Rightarrow$$

$$T(j\omega) = - \frac{1}{-\omega^2 R_1^2 C_1^2} \cdot \frac{1+j\omega R_1C_1}{1+j\omega R_2C_2} ; T(j\omega) = 1 \Rightarrow$$

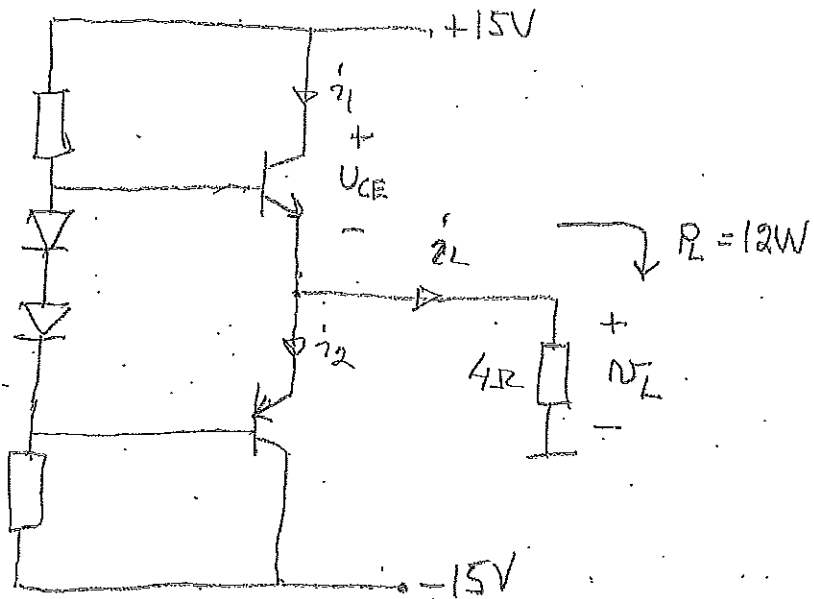
$$\bullet R_1 C_1 = R_2 C_2 \quad \bullet \omega^2 R_1^2 C_1^2 = 1 \Rightarrow$$

$$C_1 = \frac{R_2 C_2}{R_1} = \frac{1,5 \text{ k}\Omega}{8,2 \text{ k}\Omega} \cdot 22 \text{ nF} = \underline{\underline{4,02 \text{ nF}}}$$

$$\omega = \frac{1}{R_1 C_1} = \frac{1}{8,2 \cdot 10^3 \cdot 4,02 \cdot 10^{-9}} = \underline{\underline{30,3 \text{ rad/s}}} \Rightarrow$$

$$f = \underline{\underline{4,82 \text{ kHz}}}$$

5



$$P_L = 4\Omega \cdot \frac{i_L^2}{2} \Rightarrow \frac{i_L}{2} = \sqrt{\frac{2 \cdot 12W}{4\Omega}} = 2,45A$$

$$\Rightarrow i_1 = 2,45A$$

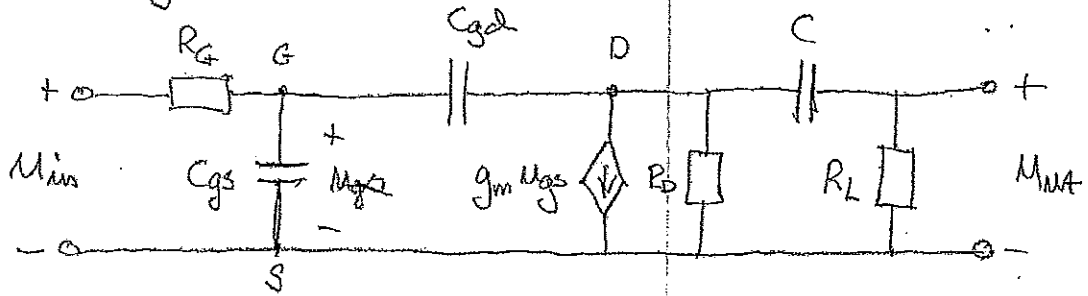
$$P_{im} = 2 \cdot 15V \cdot \frac{i_1}{\pi} = 30V \cdot \frac{2,45A}{\pi} = 23,39W \Rightarrow$$

$$\eta = \frac{P_L}{P_{im}} = \frac{12W}{23,39W} = 51,3\%$$

$$P_{T \text{ transistor}} = \frac{P_{im} - P_L}{2} = 5,70W$$

$$P_{L \text{ max}} = \frac{(V_{L \text{ max}})^2}{2 \cdot 4\Omega} = \frac{(15V)^2}{2 \cdot 4\Omega} = 28,1W$$

6. Småsignalschema



$$R_G = 800 \Omega, R_D = 4 \text{ k}\Omega, R_L = 4 \text{ k}\Omega, C = 200 \text{ nF}$$

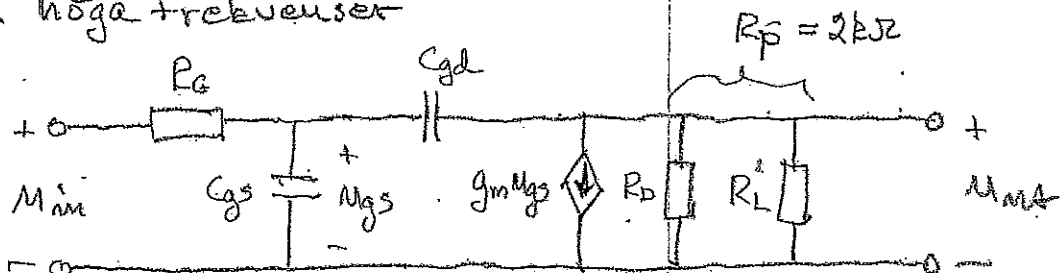
$$g_m = 40 \text{ mA/V}, C_{gs} = 30 \text{ pF}, C_{gd} = 4 \text{ pF}$$

Vi delar upp beräkningen i

a. höga frekvenser (betyder $\frac{1}{\omega C} \approx 0, \frac{1}{\omega C_{gs}} > 0, \frac{1}{\omega C_{gd}} > 0$)

b. låga frekvenser (betyder $\frac{1}{\omega C} > 0, \frac{1}{\omega C_{gs}} = \frac{1}{\omega C_{gd}} = \infty$)

a. höga frekvenser



C_{gd} delas approximativt upp med Millers sats

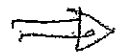
$$C_{M1} = (1 - k) C_{gd} ; C_{M2} = (1 + \frac{1}{k}) C_{gd} \text{ där}$$

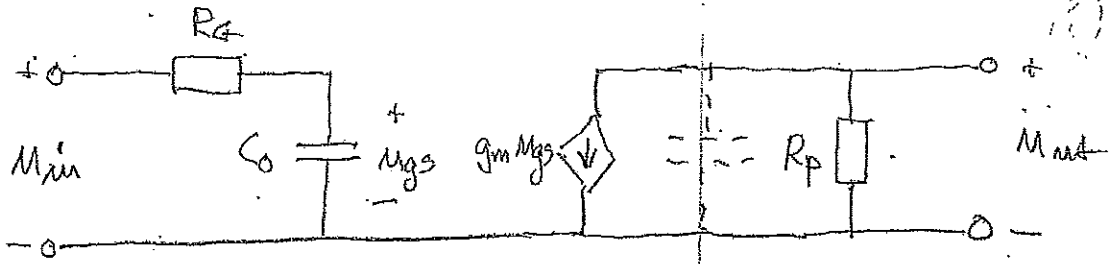
$$k \approx \frac{U_{out}}{U_{gs}} (\text{utan } C_{gd}) = \frac{-g_m U_{gs} \cdot R_p}{U_{gs}} = -g_m \cdot R_D // R_L =$$

$$\approx -40 \text{ mA/V} \cdot (4 \text{ k}\Omega // 4 \text{ k}\Omega) = -80 \text{ ggr} \Rightarrow$$

$$C_{M1} = 81 \cdot 4 \text{ pF} = \underline{324 \text{ pF}}, C_{M2} = (1 + \frac{1}{81}) \cdot 4 \text{ pF} \approx \underline{4,05 \text{ pF}}$$

Inverkan av C_{M2} försummas ofta eftersom den ger en pol flera 10-potenser högre än C_{M1} .





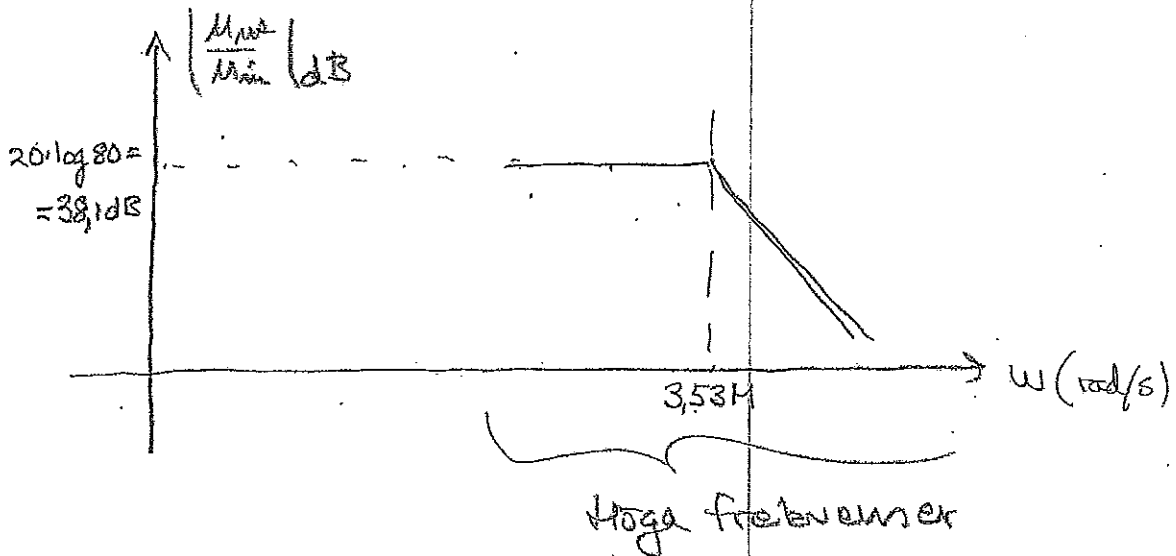
$$C_0 = C_{in1} + C_{gs} = 324 \text{ pF} + 30 \text{ pF} = 354 \text{ pF}$$

$$M_{out} = -g_m v_{gs} R_p$$

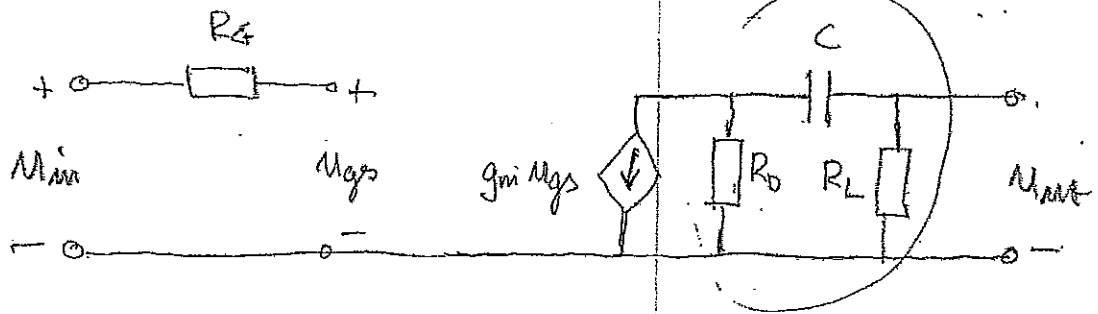
$$v_{gs} = \frac{\frac{1}{sC_0}}{R_g + \frac{1}{sC_0}} \cdot M_{in} = \frac{1}{1 + sR_g C_0} \cdot M_{in} \Rightarrow$$

$$\frac{M_{out}}{M_{in}} = -\frac{g_m R_p}{1 + sR_g C_0} = -\frac{40 \text{ mA/V} \cdot 2 \text{ k}\Omega}{1 + s \cdot 800 \Omega \cdot 354 \cdot 10^{-9} \text{ F}}$$

$$= -\frac{80}{1 + \frac{s}{3,53 \cdot 10^6}} \Rightarrow \text{Denaturens gränsvinkel-} \\ \text{frekvensen är} \\ \omega_0 = 3,53 \text{ Mrad/s}$$



b. låga frekvenser



Spänningsdelning ger

$$U_{ut} = \frac{R_L}{R_L + \frac{1}{sC}} \cdot (-g_m U_{gs} \cdot Z) = -\frac{g_m s R_L C \cdot Z}{1 + s R_L C} \cdot U_{gs}$$

$$Z = R_D \parallel \left(R_L + \frac{1}{sC} \right) = \frac{R_D \cdot \left(R_L + \frac{1}{sC} \right)}{R_D + R_L + \frac{1}{sC}}$$

$$= \frac{R_D (1 + s R_L C)}{1 + s (R_D + R_L) \cdot C} \quad U_{gs} = U_{in} \Rightarrow$$

$$U_{ut} = -\frac{g_m s R_L C \cdot R_D (1 + s R_L C)}{(1 + s R_L C)(1 + s (R_D + R_L) C)} \cdot U_{in} = -\frac{g_m R_D R_L \cdot s C}{1 + s (R_D + R_L) C} \cdot U_{in}$$

$$= -\frac{40 \text{ mA/V} \cdot 4 \text{ k}\Omega \cdot 4 \text{ k}\Omega \cdot 200 \text{ nF} \cdot s}{1 + s (4 \text{ k}\Omega + 4 \text{ k}\Omega) \cdot 200 \text{ nF}} = -\frac{\frac{s}{7.81}}{1 + \frac{s}{6.25}}$$

$$= -80 \cdot \frac{\frac{s}{6.25}}{1 + \frac{s}{6.25}}$$

Detta ger max-förstärkning $80 \text{ ggr} = 38 \text{ dB}$,
Undre grännsfrekvensen blir $\omega_u = 6.25 \text{ rad/s}$.



⇒ Hela Bode-diagrammet

