Examination	**ENM061 Power Electronic Converters**
Date and time	Saturday January 19th, 2019, 14:00 – 18:00
Teacher responsible:	Mebtu Beza/Zeyang Geng, mobile no. +46767655604
Authorised Aids:	Chalmers-approved calculator (Casio FX82..., Texas Instruments Ti-30..., and Sharp EL-W531...)
Grades:	U, 3, 4 or 5. (The limit for a grade of 3, 4 and 5 on the exam are 20, 30, and 40 pts., respectively. The maximum number of points in the exam is 50.)

The questions are not arranged in any kind of order and a formula sheet is attached in the last page.

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1) Briefly answer the following questions. ***(4 pts.)***

(a) What do Fourier series coefficients represent in a signal and why do we need to calculate them in the output signals of a switch-mode power converters? ***(2 pts.)***

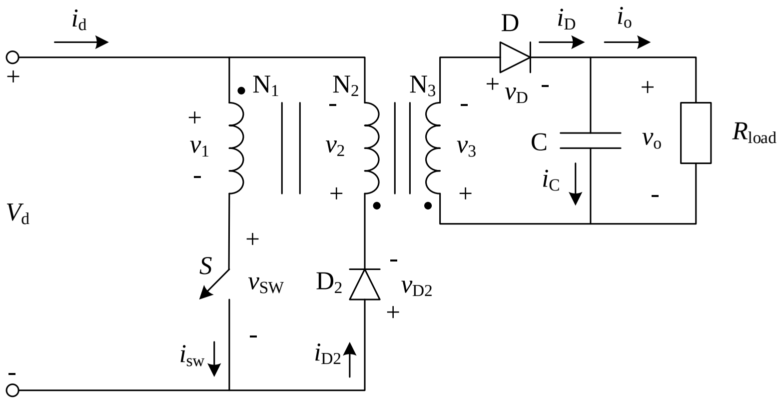
(b) Plot the Steadystate voltage-current characteristic of a MOSFET and an IGBT and describe the basic different between the two components during conduction? ***(2 pts.)***

2) The flyback converter below has a protective winding (N_2) with the total turns ratio of the transformer as $N_1{:}N_2{:}N_3 = 1{:}2{:}2$ and input voltage $V_d = 20V$. The switching frequency $f_{sw} = 20kHz$, the duty cycle $D = 0.3$ and the mutual inductance $L_m = 100\mu H$. ***(8 pts.)***

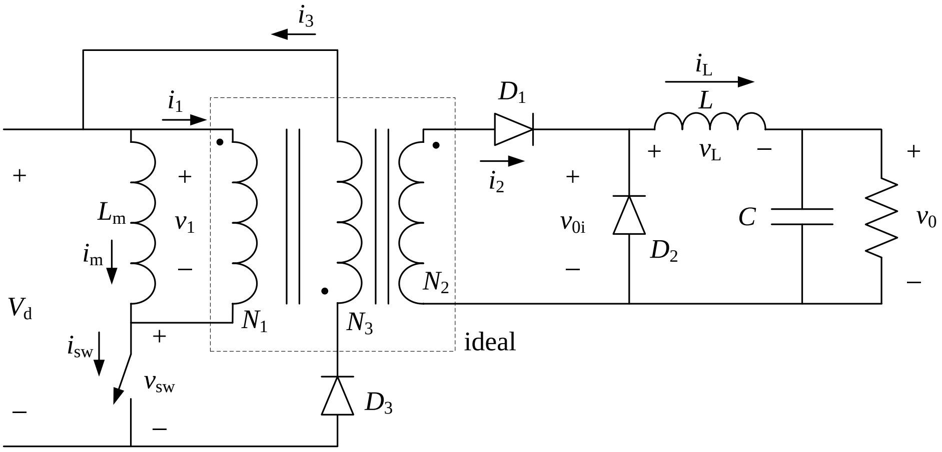
(a) For $R_{load} = 20\Omega$ and 60Ω, calculate the average output voltage V_o. ***(4 pts.)***

(b) For case a, sketch the waveforms for v_{sw}, i_d and i_D. ***(2 pts.)***

(c) What type of core excitation is used in the flyback converter transformer and is there an air-gap in the core and why? ***(2 pts.)***

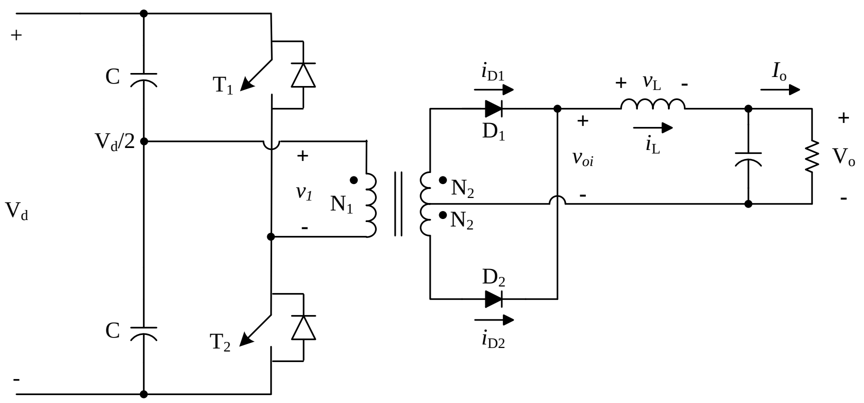


3) **The isolated 3-winding forward converter with $N_1 : N_3 : N_2 = 1 : 0.5 : 1$ shown below which basically is derived from a buck converter operates with an output voltage (V_o) of 15V and an output power (P_o) of 50 W for an input voltage (V_d) of 25V and a switching frequency (f_{sw}) of 20 kHz.** ***(11 pts.)***



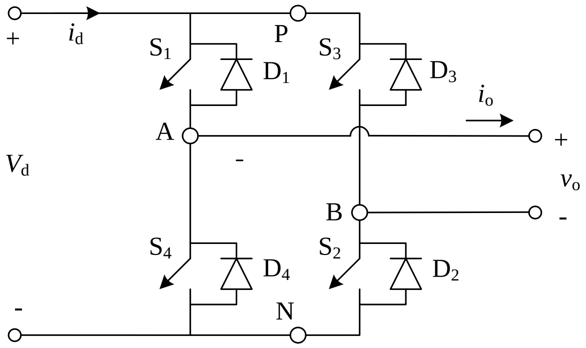
(a) Calculate the inductance (L) and the mutual inductance (L_m) in order to obtain the peak-to-peak inductor current ripple and magnetizing current ripple to be 10% and 1% of the average output current. ***(3 pts.)***
(b) Plot the inductor and capacitor current waveforms as well as i_1, i_3, i_m and v_{sw} for one switching cycle. Show the important points clearly. ***(4 pts.)***
(c) Calculate the minimum capacitance (C) in order to limit the maximum peak-to-peak output voltage ripple to 1% of the average output voltage. ***(2 pts.)***
(d) What type of core excitation is used in the forward converter transformer and is there an air-gap in the core and why? ***(2 pts.)***

4) **For the half-bridge DC/DC converter shown below operating in continuous conduction mode (CCM),** ***(6 pts.)***



(a) Roughly sketch the waveforms for i_L, i_{D1} and i_{D2} for one switching cycle. ***(2 pts.)***
(b) Derive the expression for the output to input voltage ratio (V_o/V_d). ***(2 pts.)***
(c) Roughly sketch the magnetizing current waveform and indicate what type of core excitation is used in the transformer. What is the advantage of having this type of core excitation? ***(2 pts.)***

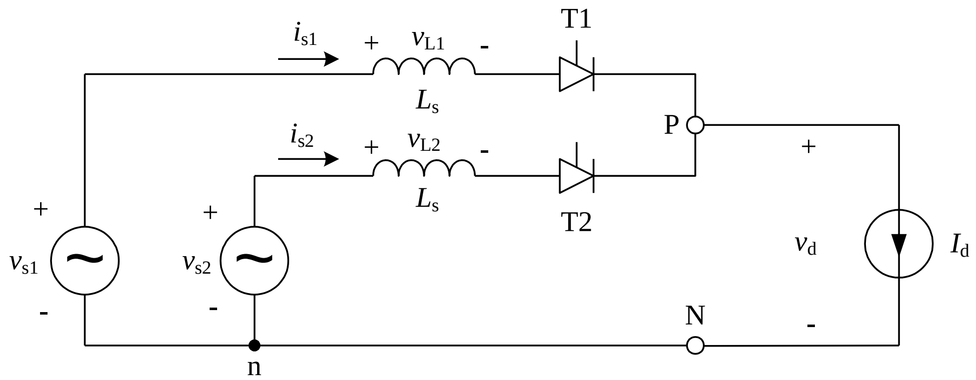
5) For the single-phase inverter shown below with an input voltage $V_d = 300V$, *(10 pts.)*



(a) For a square-wave operation, plot the output voltage waveform and calculate the magnitude of the fundamental component as well as the total harmonic distortion. ***(3 pts.)***
(b) For a square wave operation, which order of harmonics is present in the output ac-current? Can you explain what the impact of using a 3-phase inverter on these harmonics is? ***(3 pts.)***
(c) Using the inverter above, how can we improve the low-order harmonic content of the output voltage? ***(2 pts.)***
(d) What are the advantages and disadvantages of using a multilevel inverter instead of a two-level inverter as shown above? ***(2 pts.)***

6) The thyristor rectifier circuit shown below is connected to the two-phases of a 50 Hz, 230 V (RMS) three-phase voltage sources, v_{s1} and v_{s2} with a phase shift of 120°. Assume that the source inductance (L_s) is 5 mH and that $I_d = 10A$ (current-stiff source). For a delay angle (α) of 35°**, *(11 pts.)***

(a) plot i_{s1}, i_{s2}, v_d and calculate the average value of V_d. ***(5 pts.)***
(b) Calculate the average value of V_d if the delay angle changes to 145°. ***(3 pts.)***
(c) plot i_{s1}, i_{s2}, v_d and calculate the average value of V_d if the thyristors are changed to diodes and the source inductances are negligible. ***(3 pts.)***



Formula sheet for the final exam of Power Electronic Converters (ENM061)

Fourier calculations

Table 3-1 Use of Symmetry in Fourier Analysis

Symmetry	*Condition Required*	a_h and b_h
Even	$f(-t) = f(t)$	$b_h = 0 \quad a_h = \frac{2}{\pi}\int_0^{\pi} f(t)\cos(h\omega t)\, d(\omega t)$
Odd	$f(-t) = -f(t)$	$a_h = 0 \quad b_h = \frac{2}{\pi}\int_0^{\pi} f(t)\sin(h\omega t)\, d(\omega t)$
Half-wave	$f(t) = -f(t + \frac{1}{2}T)$	$a_h = b_h = 0$ for even h $a_h = \frac{2}{\pi}\int_0^{\pi} f(t)\cos(h\omega t)\, d(\omega t)$ for odd h $b_h = \frac{2}{\pi}\int_0^{\pi} f(t)\sin(h\omega t)\, d(\omega t)$ for odd h
Even quarter-wave	Even and half-wave	$b_h = 0$ for all h $a_h = \begin{cases} \frac{4}{\pi}\int_0^{\pi/2} f(t)\cos(h\omega t)\, d(\omega t) & \text{for odd } h \\ 0 & \text{for even } h \end{cases}$
Odd quarter-wave	Odd and half-wave	$a_h = 0$ for all h $b_h = \begin{cases} \frac{4}{\pi}\int_0^{\pi/2} f(t)\sin(h\omega t)\, d(\omega t) & \text{for odd } h \\ 0 & \text{for even } h \end{cases}$

Definition of RMS-value:

$$F_{RMS} = \sqrt{\frac{1}{T}\int_{t_o}^{t_o+T} f(t)^2 dt}$$

Definition of RMS-value with Fourier-series:

$$F_{RMS} = \sqrt{F_0^2 + \sum_{n=1}^{\infty} F_n^2} = \sqrt{\left(\frac{a_0}{2}\right)^2 + \sum_{n=1}^{\infty}\left(\frac{\sqrt{a_n^2 + b_n^2}}{\sqrt{2}}\right)^2}$$

Trigonometry

$$\sin^2(\alpha) + \cos^2(\alpha) = 1$$

$$\sin(\alpha+\beta) = \sin(\alpha)\cos(\beta) + \cos(\alpha)\sin(\beta)$$

$$\sin(\alpha-\beta) = \sin(\alpha)\cos(\beta) - \cos(\alpha)\sin(\beta)$$

$$\cos(\alpha+\beta) = \cos(\alpha)\cos(\beta) - \sin(\alpha)\sin(\beta)$$

$$\cos(\alpha-\beta) = \cos(\alpha)\cos(\beta) + \sin(\alpha)\sin(\beta)$$

$$\sin(\alpha)\sin(\beta) = \frac{1}{2}\left(\cos(\alpha-\beta) - \cos(\alpha+\beta)\right)$$

$$\sin(\alpha)\cos(\beta) = \frac{1}{2}\left(\sin(\alpha-\beta) + \sin(\alpha+\beta)\right)$$

$$\cos(\alpha)\cos(\beta) = \frac{1}{2}\left(\cos(\alpha-\beta) + \cos(\alpha+\beta)\right)$$

$$\int \sin(ax)dx = -\frac{1}{a}\cos(ax), \quad \int x\sin(ax)dx = \frac{1}{a^2}\left(\sin(ax) - ax\cos(ax)\right), \quad \int \cos(ax)dx = \frac{1}{a}\sin(ax)$$

$$\int x\cos(ax)dx = \frac{1}{a^2}\left(\cos(ax) + ax\sin(ax)\right)$$

$$PF = \frac{P}{S} = \frac{V_s I_{s1}\cos\phi_1}{V_s I_s}, \quad DPF = \cos\phi_1, \quad \%THD_i = 100\frac{I_{dis}}{I_{s1}} = 100\frac{\sqrt{I_s^2 - I_{s1}^2}}{I_{s1}} = 100\sqrt{\sum_{h\neq 1}\left(\frac{I_{sh}}{I_{s1}}\right)^2}$$

Electromagnetics

$$e = \frac{d}{dt}\psi \qquad \psi = N\phi \qquad \phi = BA \qquad R = \frac{l}{A\mu_r\mu_0} \qquad L = \frac{\Psi}{i}$$

$$NI = R\phi = mmf \qquad N\phi = LI \qquad L = N^2/R \qquad W = \frac{1}{2}Li^2$$

Capacitor and inductor current-voltage relationship

$$i_C = C\frac{dv_C}{dt} \qquad v_L = L\frac{di_L}{dt}$$