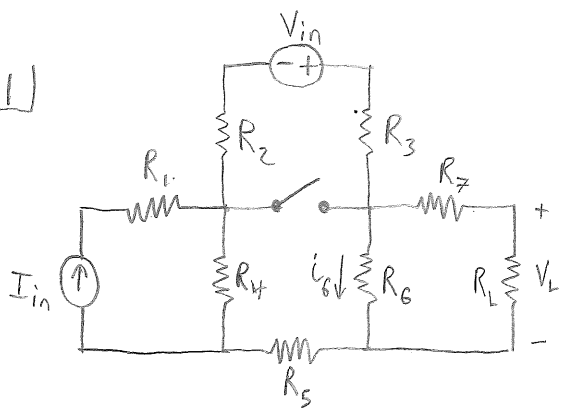


1)



a) $V_6 = i_6 R_6$

$V_L = V_6 \cdot \frac{R_L}{R_7 + R_L} \Rightarrow V_L(R_7 + R_L) = V_6 R_L$

$\Rightarrow R_L(V_6 - V_L) = V_L R_7 \Rightarrow \boxed{R_L = \frac{V_L R_7}{(V_6 - V_L)}}$

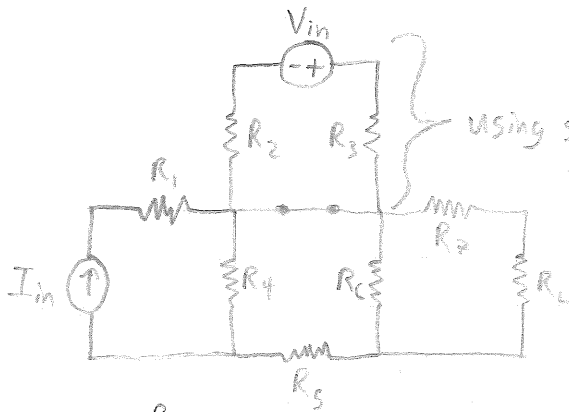
b) $\boxed{i_{V_{in}} = i_6 + \frac{V_L}{R_L}}$

$V_{in} = i_{V_{in}} R_3 + i_{V_{in}} (R_6 \parallel (R_7 + R_L)) + i_{V_{in}} R_5 + (i_{V_{in}} - I_{in}) R_4 + i_{V_{in}} R_2$

$= i_{V_{in}} (R_2 + R_3 + R_4 + R_5 + (R_6 \parallel (R_7 + R_L))) - I_{in} R_4$

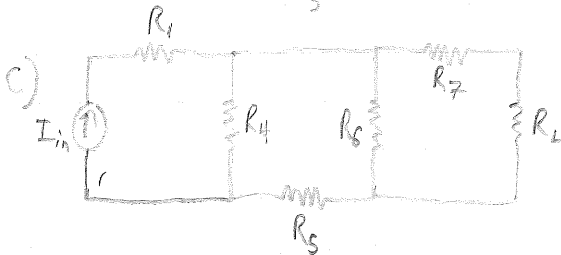
$\boxed{V_{I_{in}}} = I_{in} R_1 + (I_{in} - i_{V_{in}}) R_4$

$\boxed{P_{supplied}} = V_{I_{in}} \cdot I_{in} + V_{in} i_{V_{in}}$



Using superposition, we can see that closing the switch shorts the circuit, therefore current across R_2 and R_3 is only from V_{in} , and current across all other resistors is only from I_{in} .

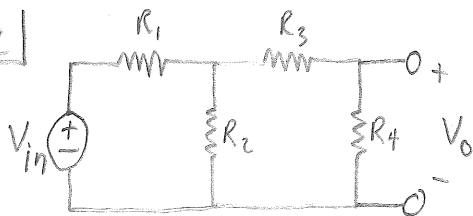
$\therefore \boxed{P_{R_2}(V_{in}) = 0 \text{ W}}$



$i_5 = \frac{I_{in} R_4}{R_4 + (R_5 + R_6 \parallel (R_7 + R_L))}$

$i_L = \frac{i_5 R_6}{R_6 + R_7 + R_L} \quad \boxed{V_L = i_L R_L}$

2)



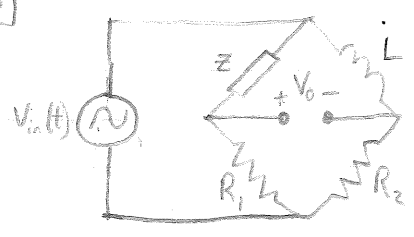
a) $V_2 = \frac{V_{in} (R_2 \parallel (R_3 + R_4))}{R_1 + R_2 \parallel (R_3 + R_4)} \Rightarrow$

$\boxed{V_0 = \frac{V_2 R_4}{R_3 + R_4} = V_{Th}}$

$\boxed{R_{eq} = R_4 \parallel (R_3 + R_1 \parallel R_2)}$

b) $\boxed{V_5 = \frac{V_0 R_5}{R_{eq} + R_5}}$

3



a) $Z_L = j\omega L$

$V_{in}(t) = I_1(t)(Z + R_1) = I_2(t)(Z_L + R_2) \Rightarrow I_2 = I_1 \frac{Z + R_1}{Z_L + R_2}$

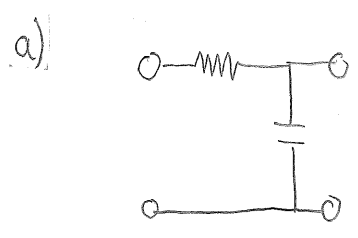
$V_o + I_2 R_2 - I_1 R_1 = 0 \Rightarrow I_1 R_1 = I_2 R_2 \Rightarrow I_2 = I_1 \frac{R_1}{R_2}$

$I_1 \frac{R_1}{R_2} = I_1 \frac{Z + R_1}{Z_L + R_2} \Rightarrow Z + R_2 = \frac{R_1}{R_2} Z_L + R_1 \Rightarrow \boxed{Z = \frac{R_1}{R_2} Z_L}$

b) Inductor: $L_{eq} = \frac{Z}{j\omega}$

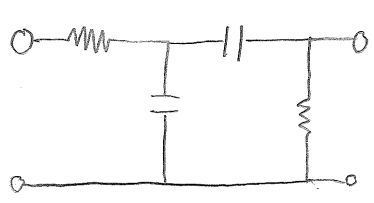
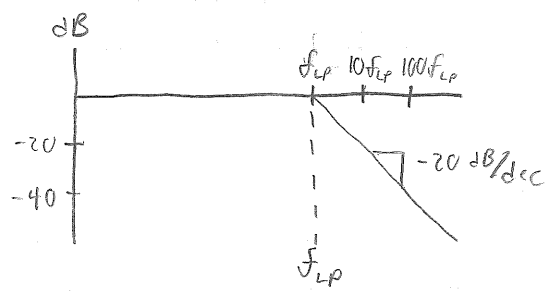
c) $Z_{eq} = (Z + R_1) \parallel (Z_L + R_2)$ $I_m = \frac{V_m}{|Z_{eq}|}$ $|S| = \frac{V_m \cdot I_m}{Z}$

4



1st order Low-Pass filter

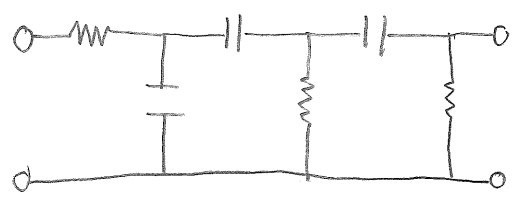
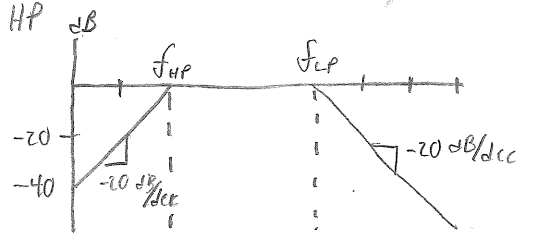
$f_{B,LP} = (Z \parallel RC)^{-1}$



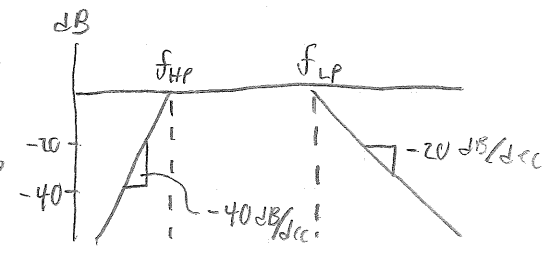
1st order LP + 1st order HP
or

1st order Band-Pass

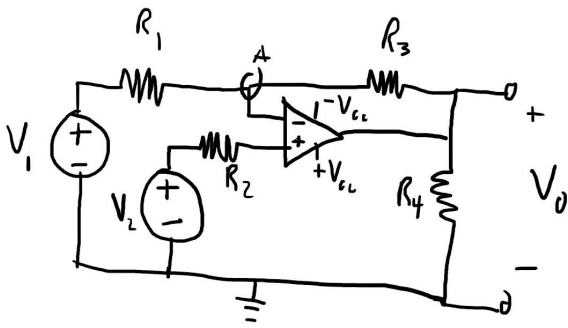
$f_{B,HP} = (Z \parallel RC)^{-1}$



1st order LP
+
2nd order HP



5



$$a) V_A = V_2$$

$$\frac{V_1 - V_2}{R_1} + \frac{V_0 - V_2}{R_3} = 0$$

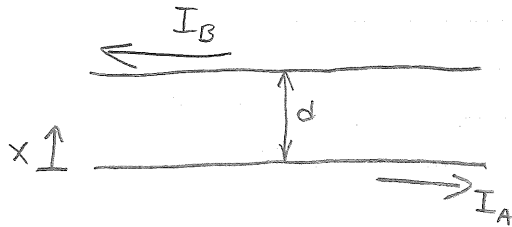
$$V_0 = V_2 \left(1 + \frac{R_3}{R_1}\right) - V_1 \left(\frac{R_3}{R_1}\right)$$

$$b) V_1 \in [-V_1, V_1]$$

$$V_2 \in [-V_2, V_2]$$

$$|V_{cc}| \geq V_0(V_1, V_2)$$

6



a)

$$\vec{B} = \int d\vec{B} = \frac{\mu_0 I}{4\pi r} \int \frac{d\vec{J} \times \hat{r}}{r^2} \xrightarrow{\text{Infinite wire}} |\vec{B}| = \frac{\mu_0 I}{4\pi r} \frac{2}{r} = \frac{\mu_0 I}{2\pi r}$$

$$\vec{B}(x) = \vec{B}_A(x) + \vec{B}_B(x) = \frac{\mu_0 I_A}{2\pi x} + \frac{-\mu_0 I_B}{2\pi(x-d)} = \frac{\mu_0 I}{2\pi} \left(\frac{1}{x} - \frac{1}{x-d} \right)$$

b)

$$d = 0$$